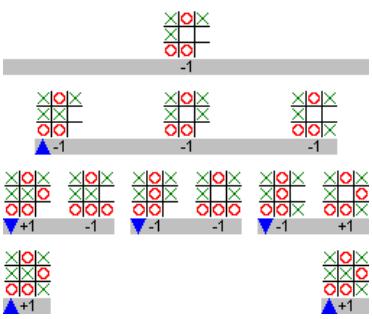


## Games

### Tic-Tac-Toe



backtracking algoritme met minimax strategie!

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## minimax

```
int TicTacToe::chooseMove(Side s,
    int& bestRow, int& bestColumn) {
    Side opp(s==COMPUTER ?
        HUMAN : COMPUTER);
    int value(s==COMPUTER ?
        HUMAN_WIN : COMPUTER_WIN);
    int simpleEval(positionValue());
    if (simpleEval==UNCLEAR)
        return simpleEval;
    for (int r(0); r<board.numrows(); ++r)
        for (int c(0); c<board.numcols(); ++c)
            if (squaresEmpty(r, c)) {
                place(r, c, s);
                int dc;
                int reply(chooseMove(opp, dc, dc));
                place(r, c, EMPTY);
                if (s==COMPUTER && reply>value ||
                    s==HUMAN && reply<value) {
                    value=reply;
                    bestRow=r;
                    bestColumn=c;
                }
            }
    return value;
}
```



## TTT

aantal aanroepen  
chooseMove bij eerste zet  
(computer begint)

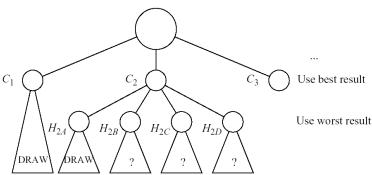
- Maximaal:  $1+9+9 \times 8+9 \times 8 \times 7+\dots+9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1 = 986410$
- Stoppen als er een winnaar is = 549946
- Toepassen alpha-beta pruning = 18297
- Toepassen transposition table = 7954
- Zoek identieke stellingen (draaien en spiegelen) = ???

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## Games

### Alpha-Beta pruning



Zie p. 398.

After  $H_{2A}$  is evaluated,  $C_2$ , which is the minimum of the  $H_2$ 's, is at best a draw. Consequently, it cannot be an improvement over  $C_1$ . We therefore do not need to evaluate  $H_{2B}$ ,  $H_{2C}$ , and  $H_{2D}$ , and can proceed directly to  $C_3$ .

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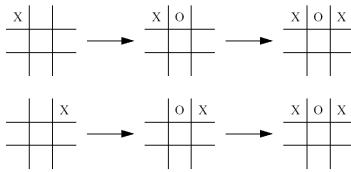
## alpha-beta

```
int TicTacToe::chooseMove(Side s,
    int& bestRow, int& bestColumn,
    int alpha, int beta) {
    Side opp(s==COMPUTER ?
        HUMAN : COMPUTER);
    int value(s==COMPUTER ? alpha : beta);
    int simpleEval(positionValue());
    if (simpleEval==UNCLEAR) return simpleEval;
    for (int r(0); r<board.numrows(); ++r)
        for (int c(0); c<board.numcols(); ++c)
            if (squaresEmpty(r, c)) {
                place(r, c, s);
                int reply(chooseMove(opp, dc, dc,
                    alpha, beta));
                place(r, c, EMPTY);
                if (s==COMPUTER && reply>value ||
                    s==HUMAN && reply<value) {
                    value=reply;
                    if (s==COMPUTER) alpha=value;
                    else beta=value;
                    bestRow=r; bestColumn=c;
                    if (alpha>=beta) return value;
                }
            }
    return value;
}
```



## Games

### Transpositions



Zie p. 400.  
Two searches that arrive at identical positions.

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## transpositions

```
class Position {
public:
    Position(const matrix<int>& theBoard):
        board(theBoard) {}
    bool operator<(const Position& rhs) const;
private:
    matrix<int> board;
};

bool Position::operator<(const Position &rhs)
const {
    for (int i(0); i<board.numrows(); ++i)
        for (int j(0); j<board.numcols(); ++j)
            if (board[i][j]<rhs.board[i][j])
                return board[i][j]<rhs.board[i][j];
    return false;
}

class TicTacToe {
//...
private:
    map<Position, int> transpositions;
};

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```

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## transpositions

```
int TicTacToe::chooseMove(Side s,
    int& bestRow, int& bestColumn,
    int alpha, int beta, int depth) {
    Position thisPosition(board);
    if (depth>=3 && depth<=5) {
        MapItr itr(transpositions.find(thisPosition));
        if (itr!=transpositions.end())
            return (*itr).second;
    }
    // idem ...
    int reply(chooseMove(opp, dc, dc,
        alpha, beta, depth+1));
    // idem ...
    if (alpha>=beta) goto Done;
}
Done:
if (depth>=3 && depth<=5)
    transpositions[thisPosition]=value;
return value;
}
```

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